

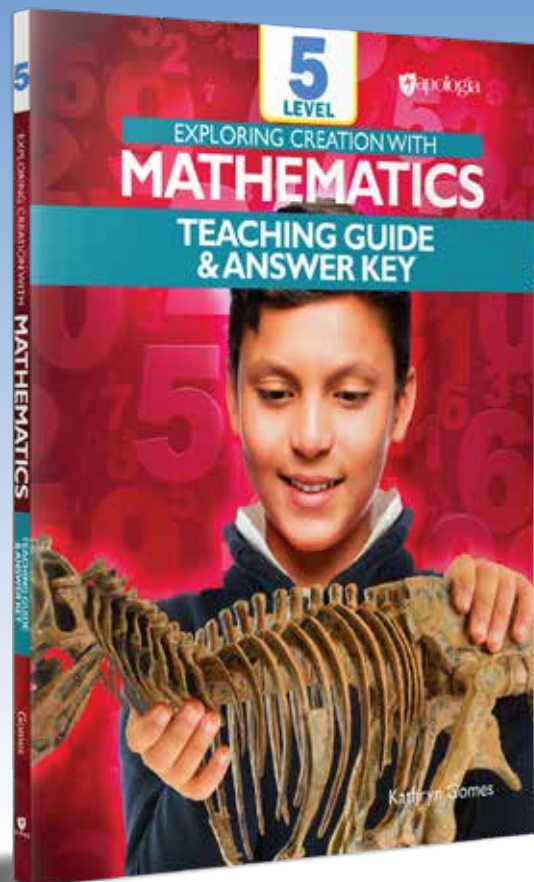
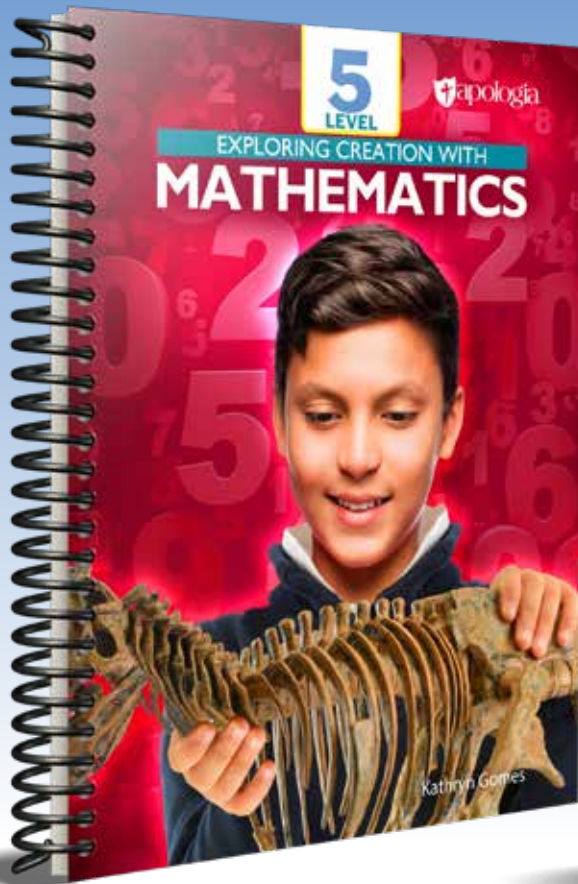


 apologia.

EXPLORING CREATION WITH
MATHEMATICS



Kathryn Gomes



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PLACE VALUE AND POWERS OF TEN

In this chapter, you will learn to:

- Follow the order of operations
- Use powers of ten and expanded form to write numbers
- Use scientific notation





LESSON 1: PLACE VALUE REVIEW

Place Value Detective

You Will Need:

- Place Value Activity Sheets (in the back of the answer key)
- Masking tape
- Scissors
- A prize (see note in the answer key)

You Will Do:

1. Have your parent set up this activity according to the instructions in the answer key.
2. Start on the paper marked “start” and read the clues. Use your knowledge of place value and numbers to guess the correct number.
3. Find the next activity sheet that has the same number as your answer on the top. Unfold it to read a new set of clues and guess the next number.
4. Continue working like this until you have guessed all the numbers. The last answer will lead you to a prize.



Place value is the value of each digit in a number. It is the system that we use to write down numbers, and the location of each digit affects its value. Each group of 3 digits is called a **period**, is separated by a comma, and follows a pattern of ones, tens, and hundreds.



PLACE VALUE:

A system of writing numbers where the location of a digit affects its value

PERIOD:

Each group of 3 digits separated by a comma

Review the place value chart below.

PLACE VALUE CHART

Millions			Thousands			Ones		
Hundred Million	Ten Million	One Million	Hundred Thousand	Ten Thousand	One Thousand	Hundreds	Tens	Ones
1	2	3,	4	5	6,	7	8	9

STANDARD FORM:

123,456,789

EXPANDED FORM:

$100,000,000 + 20,000,000 + 3,000,000 + 400,000 + 50,000 + 6,000 + 700 + 80 + 9$

WORD FORM:

one hundred twenty-three million, four hundred fifty-six thousand, seven hundred eighty-nine

Millions Period			Thousands Period			Ones Period		
1	2	3	4	5	6	7	8	9

One (s)
Ten (s)
Hundred (s)

One
Ten
Hundred

One
Ten
Hundred

We can write numbers in standard form using place value. We can also use expanded form as another way of representing the value of the number.

EXAMPLE 1: Rewrite the number 87,045 in expanded form.

$$80,000 + 7,000 + 40 + 5$$

The expanded form of the number shows exactly how many ten thousands, thousands, tens, and ones are in the number.



1. Write each number in expanded form.

a. 543,788

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}} \\ + \underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}}$$

b. 23,451

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}} \\ + \underline{\hspace{2cm}} + \underline{\hspace{2cm}}$$

c. 5,699

$$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}} + \underline{\hspace{2cm}}$$

2. Write each number in standard form.

a. $300,000 + 70,000 + 1,000 + 300 + 30 + 1 =$ _____

b. $20,000 + 4,000 + 500 + 4 =$ _____

3. Write the value of the underlined digit.

a. **2**3,800 _____

b. **8**99,107 _____

c. **1**7,845 _____

d. **2**39,980 _____

- 3. It is hard to know exactly, but some scientists believe that there are at least eight million, seven hundred thousand different species of animals on Earth. Circle the number below that correctly shows that amount.**

- a. 870,000
b. 8,700,000
c. 8,070,000



Life is abundant on Earth.



LESSON 2: ORDER OF OPERATIONS

Order Matters

You Will Do:

1. Take a trip in the car with your parents. Ask them about the rules at the intersections you encounter. Who gets to go first? What is the order for traffic flow?
2. Discuss with your parents if they have ever driven somewhere with different rules. Some countries drive on the opposite side of the street than where people drive in the United States.
3. Why do you think we have to have certain rules for the order of driving? Talk it over with your parents. Do you think it is important to follow the rules of the road?



Just like in driving, mathematicians have rules for the order in which we do math. Otherwise, there could be a lot of confusion and possibly a catastrophe! It is important that we all agree on how to do a certain problem or else we will get different answers, and we won't be able to work together.

Look at the two problems below as an example.

Micah's Work

$$4 + 2 \times 3$$

$$6 \times 3$$

$$18$$

Isaiah's Work

$$4 + 2 \times 3$$

$$4 + 6$$

$$10$$

Micah and Isaiah both worked on the same problem. They didn't make any mistakes when they added or multiplied, but they got two completely different answers. This is because they did the problem in a different order. Micah added 4 and 2 before multiplying by 3. Isaiah multiplied 2 and 3 before adding 4. Who has the correct answer?

Long ago, mathematicians noticed this problem and decided that we need to all agree on an order. They call it the **order of operations**. This order of operations is what all mathematicians follow so that we know we will all get the same answer when performing mathematical operations. In this book, we will learn 3 steps in the order of operations.

You will learn about the first step (grouping symbols) in the next lesson. The last 2 steps show that if there are 2 or more operations in a problem, you should do all the multiplication and division before you go back and do all of the addition and subtraction. It is also important that you always work from left to right. This isn't hard to remember because you read from left to right. Math is the same. Multiply and divide from left to right. Then go through and add and subtract from left to right.

Look back at the work Micah and Isaiah did. Who got the correct answer? I hope you see and understand that Isaiah's answer is the correct one.

Going left to right, Isaiah did the multiplication first. Then going left to right, Isaiah did the addition second. Now you know that following the rules is very important in math if we all want to find the same value.

When you find the value of a numerical expression, it is called **evaluating** a numerical expression. It is just a more mathematical way of saying "find the value by doing all the operations in the right order."

The Order of Operations

1. Perform operations that are in grouping symbols such as parentheses
2. Multiply and Divide (from left to right)
3. Add and Subtract (from left to right)



THE ORDER OF OPERATIONS: an agreed upon order for doing math problems

EVALUATE: To find the value of an expression

EXAMPLE 1: Evaluate the expression.

$$3 \times 5 + 2 \times 4$$

First you need to do the multiplication from left to right. To help us remember this, we can put parentheses around the multiplication operations. After we multiply we will add.

$$(3 \times 5) + (2 \times 4)$$

$$15 + (2 \times 4)$$

$$15 + 8$$

$$23$$

EXAMPLE 2: Evaluate the expression.

$$6 + 10 \times 8 - 2$$

$$6 + (10 \times 8) - 2$$
 Start with the multiplication. Draw in parentheses if that helps you.

$$6 + 80 - 2$$
 Now do the addition because it is on the left.

$$86 - 2$$
 Finally, subtract.

$$84$$

EXAMPLE 3: Evaluate the expression.

$$6 - 12 \div 4 + 9$$

$$6 - (12 \div 4) + 9$$
 Write parentheses around the division so that you remember to do that operation first.

$$6 - 3 + 9$$
 Next subtract because we move from left to right.

$$3 + 9$$
 Finally, add.

$$12$$

Notice that if you tried to add $3 + 9$ first it would have been a different answer. Students often forget to add and subtract moving from left to right.



“Do multiplication and division from left to right.
Then do addition and subtraction from left to right.”



1. Follow the order of operations to evaluate each expression. Show each step of your work.

a. $3 \times 4 + 5$

b. $7 - 2 \times 3$

c. $10 - 8 + 6$

d. $4 + 16 \div 4$

e. $3 \times 8 + 7 \times 2$

f. $10 + 72 \div 9$

g. $24 \div 6 + 4 \times 2$

h. $8 + 5 \times 4 - 5$

i. $6 + 10 \times 5 - 3$

j. $5 + 32 \div 4 + 3$

2. Write your own order of operations problem below. Then write the correct answer. Cover the answer with a piece of paper and see if someone can solve it correctly.



LESSON 3: PARENTHESES AND BRACKETS

Order of Operations Shuffle

You Will Need:

- Lesson 3: Activity Sheet
- Scissors
- Tape

You Will Do:

1. Have your parent tear out the activity sheet from the back of the answer key and cut the strips apart. They should scramble the strips so you do not see the original order.
2. Starting with the problem labeled “Start,” evaluate the expression and find the strip with the answer on it. Line that strip up underneath.
3. Once you have all the strips lined up, tape them together. Flip them over to see a picture.



Sometimes mathematicians want to be able to tell you to do a certain step in a problem first. Look at the situation below for an example of this.

Every week Sarah earns \$10. She spends \$3 and then puts the rest in her bank. How much money will she have after 7 weeks?

To find the answer, you need to multiply by 7 and subtract 3. If we follow the order of operations, we will multiply first and then subtract. But that is not what Sarah did. She spent the \$3 before putting the money in the bank. We need a way to show other mathematicians that they need to subtract first. They use **grouping symbols** to do this.

$$(10 - 3) \times 7$$

The parentheses above are an example of a grouping symbol. Grouping symbols direct us to a certain part of a problem that we need to do first. In this case, we need to subtract 3 before multiplying by 7.

$$(10 - 3) \times 7$$

$$7 \times 7$$

$$49$$

Sarah will have \$49 after 7 weeks.

There are different kinds of grouping symbols. Whenever you see grouping symbols, you do the math in the symbols first. Then you complete addition and multiplication and division from left to right. Finally you go back and do any addition and subtraction left to right.

If there is more than one set of grouping symbols, you start in the center and work your way out. Let's do a couple practice problems together.

Grouping Symbols

()

Parentheses

[]

Brackets



GROUPING SYMBOLS:

A set of symbols that indicate you should do certain operations first

EXAMPLE 1: Evaluate the expression. Show each step.

$$2 \times [(7 - 3) \times (2 + 2)]$$

I see brackets; we start there. But inside the brackets, I see parentheses. I must start with the expressions in the parentheses that are furthest inside first.

$$2 \times [4 \times 4]$$

Now perform the next operation. The brackets remain and I must do the math inside of them before I move on.

$$2 \times 16$$

All that is left is multiplication. I can do that easily.

$$32$$

EXAMPLE 2: Evaluate the expression. Show each step.

$$25 - [(10 \div 2) \times (10 - 7)]$$

Start with the expressions in the parentheses that are furthest inside first.

$$25 - [5 \times 3]$$

Now do the next operation that is inside the brackets.

$$25 - 15$$

Subtract

$$10$$



1. Evaluate each expression. Remember to follow the order of operations and complete steps within grouping symbols first. Show each step of your work.

The Order of Operations

1. Perform operations that are in grouping symbols such as parentheses
2. Multiply and Divide (from left to right)
3. Add and Subtract (from left to right)



a. $(5 - 2) \times (4 + 5)$

b. $(25 \div 5) + (6 \times 4)$

c. $28 \div [10 - (6 \div 2)]$

d. $3 \times [(9 - 6) + (16 \div 2)]$

e. $4 \times [(3 \times 3) - 5]$

f. $2 \times [(12 - 8) \times 2] + 3$

LESSON 4: POWERS OF TEN



Roll, Write, and Expand

You Will Need:

- 3 dice

You Will Do:

1. Roll the three dice and use the results to write a three-digit number below. Then write out the number in expanded form.
2. Roll the three dice twice and write down a six digit number in the space provided. Write out the number in expanded form.
3. Roll the three dice three times and write down a nine digit number. Write out the number in expanded form.



Number	Expanded form

_____, _____	
_____, _____, _____	

You've already reviewed the place value chart and learned about what each digit represents. But you may not have noticed the relationship between each spot on the chart. Each spot on the chart is ten times the value of the spot to its right. For instance, the 1,000 place is ten times 100 ($10 \times 100 = 1,000$). Let's look at another example.

Ones		
Hundreds	Tens	Ones
7	0	0

7,000 is ten times as big as 700.

Thousands			Ones		
Hundred Thousand	Ten Thousand	One Thousand	Hundreds	Tens	Ones
		7,	0	0	0

$$700 \times 10 = 7,000$$

In the same way, each spot on the chart is $1/10$ the value of the spot to the left. The 1,000 place is $1/10$ of the 10,000 place ($10,000 \div 10 = 1,000$). Let's look at another example.

Thousands			Ones		
Hundred Thousand	Ten Thousand	One Thousand	Hundreds	Tens	Ones
	8	0,	0	0	0

8,000 is $1/10$ as big as 80,000.

Thousands			Ones		
Hundred Thousand	Ten Thousand	One Thousand	Hundreds	Tens	Ones
		8,	0	0	0

$$80,000 \div 10 = 8,000$$

Each of the different values on the place value chart can be represented by multiplying by 10.

10

$$100 = 10 \times 10$$

$$1,000 = 10 \times 10 \times 10$$

$$10,000 = 10 \times 10 \times 10 \times 10$$

$$100,000 = 10 \times 10 \times 10 \times 10 \times 10$$

$$1,000,000 = 10 \times 10 \times 10 \times 10 \times 10 \times 10$$

BASE: The number we multiply over and over in an exponent



EXPONENT: The small number written to the right and above the base that tells us how many times to multiply

POWERS OF TEN: A number that is the product of multiplying tens

It is tiring and can be confusing to write out so many tens like that. So, mathematicians came up with a simpler way of showing that you need to multiply by the same number over and over again. The **base** is the number we multiply by over and over and the **exponent** tells us how many times to multiply.

Diagram showing the components of 10^3 :

- Exponent:** 3
- Base:** 10

This is the same as

$$10 \times 10 \times 10$$

Common Mistake:

10^3 is not the same as 10×3 .

$$10 \times 3 = 30$$

$$10^3 = 10 \times 10 \times 10 = 1,000$$

We can make a chart showing these numbers which we call the **powers of ten**.

The Powers of Ten		
10	10	10^1
100	10×10	10^2
1,000	$10 \times 10 \times 10$	10^3
10,000	$10 \times 10 \times 10 \times 10$	10^4
100,000	$10 \times 10 \times 10 \times 10 \times 10$	10^5
1,000,000	$10 \times 10 \times 10 \times 10 \times 10 \times 10$	10^6



1. Use your knowledge of place value to answer the questions below.

- a. 800 is ten times as much as what number? _____
- b. 90 is $\frac{1}{10}$ of what number? _____
- c. 60,000 is ten times as much as what number? _____
- d. 300 is $\frac{1}{10}$ of what number? _____

2. Complete the chart.

Number	Ten times as much	$\frac{1}{10}$ as much
100		
50		
8,000		
20,000		
300,000		

3. Match each number to the correct power of ten.

100	10^1
10	10^2
10,000	10^3
1,000,000	10^4
1,000	10^5
100,000	10^6

LESSON 5: POWERS OF TEN AND EXPANDED FORM



Powers of Ten Slider

You Will Need:

- Lesson 5: Activity Sheets
- Scissors

You Will Do:

1. Carefully tear out the activity sheets from the back of the answer key. Cut out the blank strips along the dotted lines. Then cut out the slider and cut slits along the dotted lines. The easiest way to do this is to fold the slider in half and cut the slits, and then unfold it.
2. Weave one of the strips into the slider so that it shows through in all of the place value windows. Write in the number 5,122. Move the decimal point in the number one space to the right by sliding the strip to the left. This also gives you the answer to $5,122 \times 10$. Write the answer below.



$$5,122 \times 10 = \underline{\hspace{2cm}}$$

3. Move the decimal point again by sliding the strip to the left one space to find the answer to $5,122 \times 100$. Write the answer below.

$$5,122 \times 100 = \underline{\hspace{2cm}}$$

4. Slide a new strip into the slider and write the number 98,000. This time we are going to move the decimal point to the left. Slide the strip to the right one space to find the answer to $98,000 \div 10$. Slide it to the right again to find the answer to $98,000 \div 100$. Write both answers below.

$$98,000 \div 10 = \underline{\hspace{2cm}} \qquad 98,000 \div 100 = \underline{\hspace{2cm}}$$

5. Slide a third strip into the slider and write a number of your choosing. Slide it to the right and to the left to write and answer two of your own problems.

$$\underline{\hspace{2cm}} \times 10 = \underline{\hspace{2cm}} \qquad \underline{\hspace{2cm}} \div 10 = \underline{\hspace{2cm}}$$

6. Keep the slider in a safe place; you will use it again in Lesson 8.

You've already learned one way to write numbers in expanded form. There are two other ways you can do this that help you see the place value relationship in different ways.

EXAMPLE 1: Write the number 76,819 in expanded form using multiplication and parentheses.

$$(7 \times 10,000) + (6 \times 1,000) + (8 \times 100) + (1 \times 10) + (9 \times 1)$$

Writing the number out in expanded form like this lets us see each power of ten. We can also write numbers in expanded form using the powers of ten notation.

EXAMPLE 2: Write the number 76,819 in expanded form using the powers of ten.

$$7 \times 10^4 + 6 \times 10^3 + 8 \times 10^2 + 1 \times 10^1 + 9$$



1. Use what you learned in the opening activity to find the answers to these problems. You can make a new strip and act it out if you need to.

a. $3,557 \times 10 =$ _____

b. $3,557 \times 100 =$ _____

c. $790,000 \div 10 =$ _____

d. $790,000 \div 100 =$ _____



2. Write each number in expanded form using multiplication and parentheses.

a. 5,671 _____

b. 10,156 _____

c. 99,678 _____

d. 566,123 _____

3. Write the each number in expanded form using the powers of ten.

a. 6,799 _____

b. 11,255 _____

c. 345,115 _____

d. 90,221 _____

4. A researcher estimates that about 291,640 platypuses live in a region of Australia. Write this estimate in expanded form using multiplication and parentheses. Then write it again using powers of ten.



The platypus is an egg-laying, semi-aquatic mammal. They have many unique and surprising characteristics that don't match with what we typically assume about mammals.



LESSON 6: SCIENTIFIC NOTATION

Powers of Ten Matching Activity

You Will Need:

- Lesson 6: Activity Sheet
- Scissors
- Glue stick

You Will Do:

1. Carefully tear out the activity sheet from the back of the answer key.
2. Cut apart the cards and scramble them.
3. Match them to their correct spots. Glue your answers from the opening activity in the spaces below.

One hundred	10^2	10×10
One thousand	10^3	$10 \times 10 \times 10$
Ten thousand	10^4	$10 \times 10 \times 10 \times 10$
One hundred thousand	10^5	$10 \times 10 \times 10 \times 10 \times 10$
One million	10^6	$10 \times 10 \times 10 \times 10 \times 10 \times 10$

100

1,000,000

100,000	

10,000	

1,000	

Powers of ten are used by scientists as well as mathematicians. Scientists use them to write very large numbers more easily. This way of writing numbers is called **scientific notation**. It can also be used to write very small numbers, but you will learn about that in the future.

In this lesson, you will practice using powers of ten and scientific notation to write large numbers. You will be practicing a math skill and a science skill at the same time.

To write a number in scientific notation, you rewrite it as a number multiplied by a power of ten. The number you are multiplying must be greater than or equal to 1 and less than 10. In other words, there can only be one digit to the left of the decimal point. Let's look at some examples to get you started.

**SCIENTIFIC NOTATION:**

A way of writing really big or really small numbers using powers of ten

EXAMPLE 1: Write the number 8,000 in scientific notation.

$$8,000$$

$$8 \times 1,000$$

$$8 \times 10^3$$

$$8,000 \text{ written in scientific notation is } 8 \times 10^3.$$

EXAMPLE 2: Write the number 2,000,000 in scientific notation.

$$2,000,000$$

$$2 \times 1,000,000$$

$$2 \times 10^6$$

EXAMPLE 3: Write the number 4×10^5 in standard form.

We know that 10^5 is 100,000. You can remember this because it has 5 zeros just like the exponent 5.

$$4 \times 100,000$$

$$400,000$$

$$4 \times 10^5 = 400,000$$

**1. Write each number in scientific notation.**

a. 900

$$\underline{\hspace{2cm}} \times 10^{\square}$$

b. 8,000

$$\underline{\hspace{2cm}} \times 10^{\square}$$

c. 4,000

$$\underline{\hspace{2cm}} \times 10^{\square}$$

d. 70,000

$$\underline{\hspace{2cm}} \times 10^{\square}$$

e. 8,000,000

$$\underline{\hspace{2cm}} \times 10^{\square}$$

f. 300,000

$$\underline{\hspace{2cm}} \times 10^{\square}$$

2. Write the each number in standard form.

a. 3×10^4 _____

b. 6×10^3 _____

3. A researcher estimated that there were 400,000 African elephants. Write this number in scientific notation.



African elephant

LESSON 7: PROBLEM SOLVING PRACTICE #1

You have done a great job so far in this chapter learning and reviewing place value. Now we are going to pause our learning of those skills to practice some general problem solving. This is different than order of operations. Perhaps you will remember from previous courses that problem solving is a strategy you develop when you work on problems that can be solved in many different ways. There isn't one certain set of steps you have to follow to get the correct answer, and you might even try several different things before you find the strategy that works for you. Let's review those steps and strategies below.

Problem Solving Process

1. Read and understand the problem.
2. Choose your strategy and make a plan.
3. Work through your plan. Change your plan and try something else if necessary.
4. Check your answer. Does it make sense?
5. Present your solution verbally or in writing.



Learning this problem solving process takes time and practice. Every time you work on one of these problems you will not only be focused on solving it, but you will be getting better at this process as well. Before jumping into the problems in the lesson, take some time to review the steps of the problem solving process in more detail.

1. Read and understand the problem.

This step might sound obvious, but it really is important. Never skip this first step. Read the problem slowly and carefully. You may want to read it through twice. I like to read problems out loud to make sure I don't rush and miss something. Underline anything you think is important information. Ask yourself, "What are they asking me to find?" and, "What information was I given?" These questions will help you form a good strategy in step 2.



2. Choose your strategy and make a plan.

You will be learning and practicing many different problem solving strategies throughout this book. You are probably already using many of them now even if you didn't know they had a specific name.



The strategy you choose is up to you, but some work better with certain problems. Here are five suggested strategies.

- Make a list or table
- Act it out
- Guess and check
- Draw a picture
- Work backwards

3. Work through your plan. Change your plan and try something else if necessary.

This is a fancy way of saying “solve the problem.” Try your plan and see if you can get an answer. If you get stuck, don’t get frustrated. That is all just part of the process. Mathematicians often have to try several different strategies before they get the right answer. Don’t be afraid to stop what you are doing and start again with a new strategy.



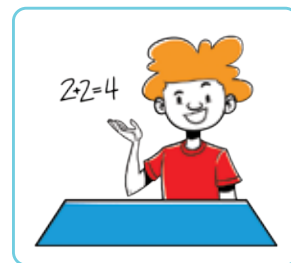
4. Check your answer. Does it make sense?

You did all that hard work, so don’t let a little addition error or something like that keep you from getting the correct answer. Double check your work and make sure your answer makes sense in the context of the problem. If you found that a person was 190 years old or that a brand new car cost \$5, you probably should look for possible mistakes.



5. Present your solution verbally or in writing.

Communication is a part of being a mathematician. Good mathematicians can clearly explain what they did so that they can work together with other mathematicians. Also, presenting your solution to someone else helps you really understand the process you went through. You may have used a piece of scratch paper to scribble out your different ideas. That is just fine, but take some time to rewrite your work neatly with the steps in order. This clarifies your thinking for yourself and others. You will have a chance to practice this skill in the problem solving lessons and in a poster presentation in the last unit of this book.



One of the coolest things about problem solving is that each mathematician has his or her own style. You might solve a problem in a completely different

way than your friend or even your mom or dad. And that isn't just ok, it's great! Creativity and innovative thinking are key components of becoming a great mathematician. You are developing your own style as a problem solver. In this book, you won't be told which type of strategy to use. Instead, it is going to be up to you. If you found the correct answer and can explain what you did to someone else, then you got it right—even if your process doesn't exactly match the answer key. Let's do one together.

EXAMPLE 1: Wesley is thinking of a number. He gives 3 clues. Can you guess his number?

1. The number is between 20 and 40.
2. It is an odd number.
3. The digits add up to 10.

Solution #1

One way to solve the problem is to use guess and check. You could use any of the clues to start your guesses. Suppose you started by thinking of a number that has digits that add to 10. You might guess 19.

This guess is too low. It is not between 20 and 40. So from there, you might decide to guess a number in the twenties with digits that add up to 10.

28

The problem with this guess is that it is even. Now try a guess in the thirties.

37

This number fits with all three clues. It is Wesley's number.

Solution #2

Making a list or table can help you organize the information. Make a list using the numbers that satisfy the first clue. The number is between 20 and 40.

21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	

The second clue says the number must be odd. Cross off all the even numbers.

21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	

The third clue says that the digits add up to 10. If you look at the remaining numbers there is only one that will work.

37

This is Wesley's number.



Solve each problem below using any strategy you like.
Once you find the answer, explain what you did to your parent.

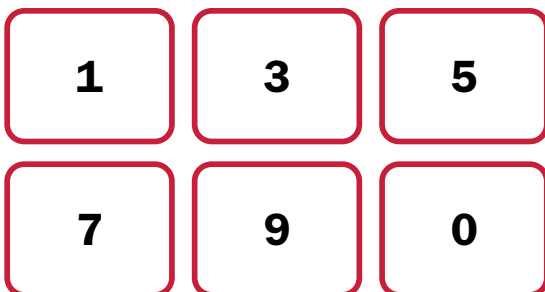
1. **Elijah is thinking of a number. He gives 3 clues.
Can you guess his number?**

My number is a two-digit number.

Both digits are the same number.

The digits add up to 12.

2. **Sam is playing with the six numbered cards shown below. He uses the card to make a subtraction problem with a difference of 854. If each card was only used once, where did he place each card in the problem?**



$$\begin{array}{r}
 \underline{\quad\quad\quad} \\
 - \quad \underline{\quad\quad\quad} \\
 \hline
 8 \quad 5 \quad 4
 \end{array}$$

SKILLS CHECK

You should have been practicing adding three-digit numbers each day as part of your skills practice. Here are a few more for you to try.

a.
$$\begin{array}{r} 415 \\ + 296 \\ \hline \end{array}$$

b.
$$\begin{array}{r} 569 \\ + 188 \\ \hline \end{array}$$

c.
$$\begin{array}{r} 205 \\ + 152 \\ \hline \end{array}$$

d.
$$\begin{array}{r} 177 \\ + 233 \\ \hline \end{array}$$

1. Write each number in expanded form using powers of ten.

a. 8,023 _____

b. 501,720 _____

2. Write each number in standard form.

a. 5×10^6 _____

b. 7×10^3 _____

3. Evaluate each expression.

a. $2 \times 3 + 4 \times 8$ _____

b. $10 - 5 + 3$ _____

c. $32 \div [9 - (10 \div 2)]$ _____

d. $4 \times [(7 - 4) + (20 \div 5)]$ _____

5
LEVEL

apologia

EXPLORING CREATION WITH
MATHEMATICS

**TEACHING GUIDE
& ANSWER KEY**



Kathryn Gomes

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WEEK-BY-WEEK DAILY SCHEDULE

Below is a suggested weekly schedule to help you stay on track. It uses a four-day week to leave room for a co-op day or a review day. This schedule covers 36 weeks, but please feel free to adjust it to the needs of your child and your family's calendar.

Week	Day 1	Day 2	Day 3	Day 4
1	UNIT 1 INTRO <input type="checkbox"/> CHAPTER 1 Lesson 1 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Lesson 2 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Lesson 3 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Lesson 4 Skills practice: adding three-digit numbers
2	CHAPTER 1 <input type="checkbox"/> Lesson 5 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Lesson 6 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Lesson 7 Skills practice: adding three-digit numbers	CHAPTER 1 <input type="checkbox"/> Chapter 1 Review
3	CHAPTER 2 <input type="checkbox"/> Lesson 8 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 9 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 10 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 11 Skills practice: subtracting three-digit numbers
4	CHAPTER 2 <input type="checkbox"/> Lesson 12 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 13 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 14 Skills practice: subtracting three-digit numbers	CHAPTER 2 <input type="checkbox"/> Lesson 15 Skills practice: subtracting three-digit numbers



TEACHER'S NOTES

UNIT 1: WHOLE NUMBERS

Unit One is a tour through many different concepts that are foundational to what we will be learning later in the year. Much of what is covered in this unit is review from 4th grade. In addition, we are going deeper into concepts like factors, multiples, and prime numbers. It is a great opportunity for kids to see the connection between different ideas like multiplication and long division. And the whole unit wraps up with an epic game of Mathematical Clue.

SUPPLY LIST

Skills Practice:

- Notecards
- Addition worksheets (on the Book Extras website)
- Uno cards
- Subtraction worksheets (on the Book Extras website)
- A four-operation calculator (add, subtract, multiply, and divide)

Chapter One:

- Masking tape
- A prize
- Scissors
- Tape
- 3 dice
- A glue stick

Chapter Two:

- Play Money (\$1's, \$10's, and \$100's)
- Scissors
- Glue
- 15 one-inch square tiles

Chapter Three:

- Play money (\$1's, \$10's, and \$100's)
- Scissors
- Glue
- Graham crackers
- Pretzel sticks
- Markers or colored pencils
- A clipboard
- Scratch paper
- 8 envelopes
- A timer

SKILLS PRACTICE FOR UNIT 1: ADDITION AND SUBTRACTION

Skill 1: Adding three-digit numbers

This skill was covered in detail in the earlier levels of this series. However, all kids can benefit from some review.

1. Notecard facts. Write a three-digit addition problem for them on a notecard and have them solve it. Rotate between problems that require regrouping and those that don't.
2. Practice with the addition worksheets that are available on the Book Extras website.
3. Play "Make the Greatest Sum." Each player picks 6 Uno cards and uses them to write an addition problem. Whoever has the largest sum wins.
4. **Take It Further:** For an extra challenge, give kids part of the addition problem and the sum. They have to work backward to find the missing part like in the example below.

$$\begin{array}{r} 729 \\ + \square\square\square \\ \hline 877 \end{array}$$

Skill 2: Subtracting three-digit numbers

The most challenging problems in this skills practice are those where you need to regroup twice or where you subtract across zeros. Some examples of those are below, followed by some suggestions on how to practice.

$$\begin{array}{r} 210 \\ - 98 \\ \hline \end{array}$$

$$\begin{array}{r} 800 \\ - 562 \\ \hline \end{array}$$

$$\begin{array}{r} 912 \\ - 198 \\ \hline \end{array}$$

$$\begin{array}{r} 502 \\ - 378 \\ \hline \end{array}$$

1. Notecard facts. Write a three-digit subtraction problem for them on a notecard and have them solve it. Rotate between problems that require regrouping and those that don't.
2. Practice with the subtraction worksheets that are available on the Book Extras website.
3. Play "Make the Greatest Difference." Each player picks 6 Uno cards and arranges them to make a subtraction problem. The player with the greatest difference wins.
4. **Take It Further:** For an extra challenge, give kids part of the subtraction problem and the difference. They have to work backward to find the missing part like in the example below. These can be pretty tough, especially if there is regrouping involved. Start with one that doesn't have regrouping and work up from there.

$$\begin{array}{r} 299 \\ - \square\square\square \\ \hline 143 \end{array}$$

$$\begin{array}{r} 803 \\ - \square\square\square \\ \hline 305 \end{array}$$

Skill 3: Multiplying by a Two-Digit Number

Students will be multiplying in Chapter 2. But most students will need additional practice to really let that skill sink in. That is why it is included in the Unit 1 skills practice.

1. Notecard problems. This is probably the easiest, most straightforward way to practice this skill. Each day, give your child one problem to complete. I like to write it out on a colorful notecard and put the answer on the back so that they can check when they are done. Below are 7 problems you could use, one for each day that they are doing this skills practice.

$$\begin{array}{r} 14 \\ \times 23 \\ \hline \end{array}$$

$$\begin{array}{r} 25 \\ \times 11 \\ \hline \end{array}$$

$$\begin{array}{r} 81 \\ \times 27 \\ \hline \end{array}$$

$$\begin{array}{r} 15 \\ \times 79 \\ \hline \end{array}$$

$$\begin{array}{r} 19 \\ \times 22 \\ \hline \end{array}$$

$$\begin{array}{r} 68 \\ \times 24 \\ \hline \end{array}$$

$$\begin{array}{r} 20 \\ \times 53 \\ \hline \end{array}$$

2. Draw and Multiply. Each player draws 4 Uno cards and uses them to create their own multiplication problem. Whoever gets the higher product wins. It is also fun to let players check their answers with a calculator.

CHAPTER 1: PLACE VALUE AND POWERS OF TEN

LESSON 1

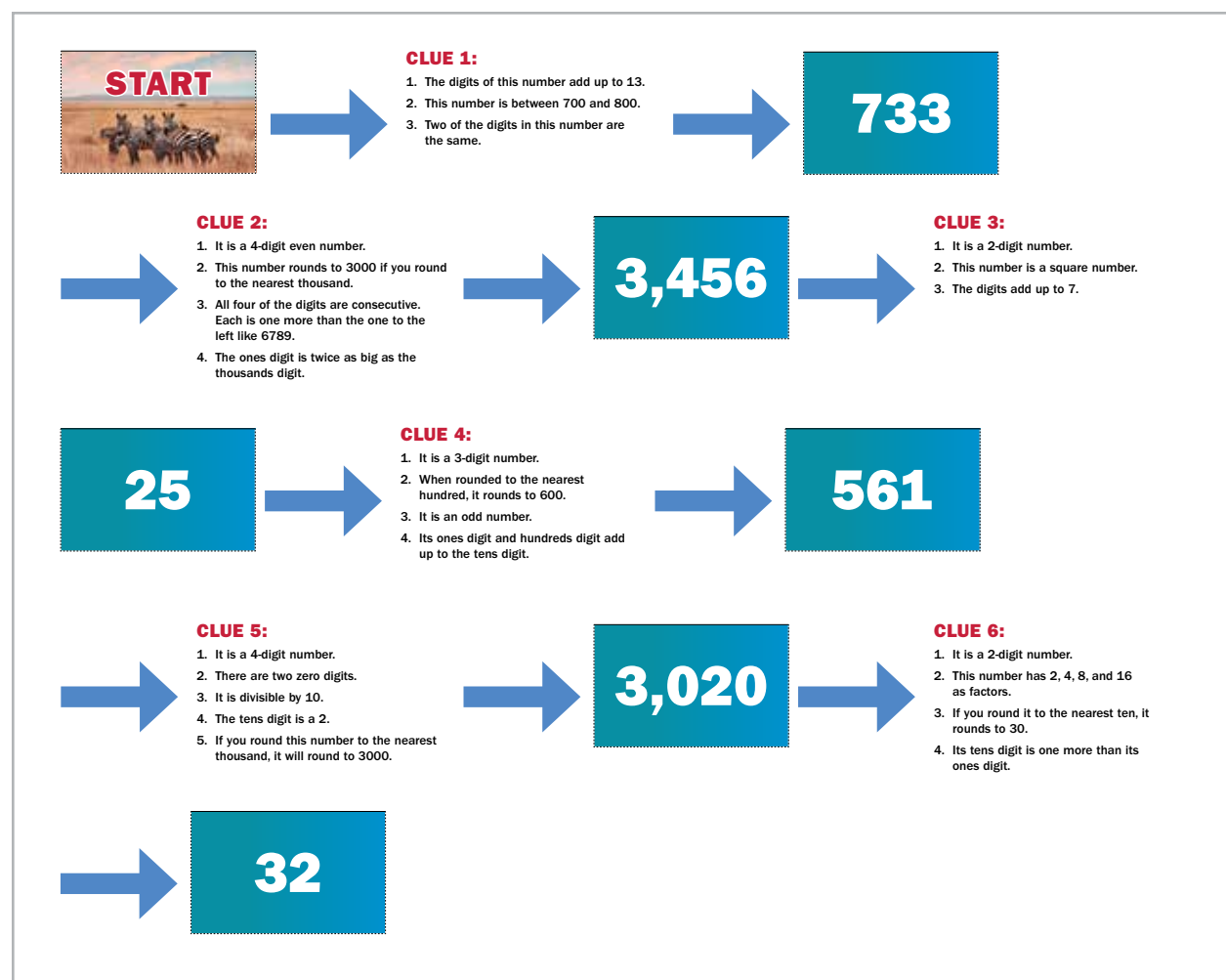
The opening activity involves some prep on your part. I promise that future activities will not be this involved; I just wanted to start the year off with something fun. I created this activity to help you hook and engage your child. Hopefully, you will agree with me that a bit more prep time was worth it.

Start by tearing out the seven activity sheets out of the back of this answer key. Cut out the squares along the dotted lines. Fold them in half along the solid black line so that the large white numbers (or the word 'start') are showing on top, and the clues are hidden inside.



Use masking tape to hang the paper at different places in your house. It could be all in the same room or you can make the search more challenging (see below). Your child will read the clues beneath the “start” paper, and then find the answer on one of the next papers. The process will continue until the last clue. It will really increase the excitement if you tape a small prize inside the final clue. This doesn’t have to be something physical. A small personal note of praise from you can even work.

Take It Further: There is only one possible answer to each clue. To make it extra challenging, space the clues throughout your house so that your child cannot see all of them at once and use the process of elimination to figure out the answers.



Page 18 Answers

LESSON 1 PLACE VALUE REVIEW

We can write numbers in standard form using place value. We can also use expanded form as another way of representing the value of the number.

EXAMPLE 1: Rewrite the number 87,045 in expanded form.
 $80,000 + 7,000 + 40 + 5$

The expanded form of the number shows exactly how many ten thousands, thousands, tens, and ones are in the number.

1. Write each number in expanded form.

a. 543,788
 $500,000 + 40,000 + 3,000 + 700 + 80 + 8$

b. 23,451
 $20,000 + 3,000 + 400 + 50 + 1$

c. 5,699
 $5,000 + 600 + 90 + 9$

Page 19 Answers

PLACE VALUE REVIEW LESSON 1

2. Write each number in standard form.

a. $300,000 + 70,000 + 1,000 + 300 + 30 + 1 = 371,331$

b. $20,000 + 4,000 + 500 + 4 = 24,504$

3. Write the value of the underlined digit.

a. 23,800 3,000

b. 899,107 800,000

c. 17,845 40


d. 239,980 900

4. It is hard to know exactly, but some scientists believe that there are at least eight million, seven hundred thousand different species of animals on Earth. Circle the number below that correctly shows that amount.

a. 870,000

b. 8,700,000

c. 8,070,000



Life is abundant on Earth.

LESSON 2

A key concept for kids to grasp is that math isn't random process. The order of operations is a set of steps that **ALL** mathematicians follow. It isn't that doing the problem another way doesn't work or doesn't make sense. It's just that everyone must agree on the same order so that answers will be consistent. Math is a language and so it has rules, the same way that English has an agreed upon set of grammar rules.

If you take the time to help your child learn the rules introduced in Level 5, the order of operations will be more manageable for them in the future as more complicated operations are added in. You might be teaching a future rocket scientist or quantum theorist, and one day they'll thank you for your diligence in helping them understand their world through the wonder of mathematics.

In the practice, kids are asked to show each step. Good mathematicians write down the process they used to solve a problem, not just the answer. This not only helps them clarify their own thinking, but also allows them to communicate their ideas clearly to others.

Page 23 Answers

ORDER OF OPERATIONS LESSON 2

1. Follow the order of operations to evaluate each expression. Show each step of your work.

a. $3 \times 4 + 5$
 $12 + 5$
 17

b. $7 - 2 \times 3$
 $7 - 6$
 1

c. $10 - 8 + 6$
 $2 + 6$
 8

d. $4 + 16 \div 4$
 $4 + 4$
 8

e. $3 \times 8 + 7 \times 2$
 $24 + 7 \times 2$
 $24 + 14$
 38

f. $10 + 72 \div 9$
 $10 + 8$
 18

g. $24 \div 6 + 4 \times 2$
 $4 + 4 \times 2$
 $4 + 8$
 12

h. $8 + 5 \times 4 - 5$
 $8 + 20 - 5$
 $28 - 5$
 23

i. $6 + 10 \times 5 - 3$
 $6 + 50 - 3$
 $56 - 3$
 53

j. $5 + 32 \div 4 + 3$
 $5 + 8 + 3$
 $13 + 3$
 16

2. Write your own order of operations problem below. Then write the correct answer. Cover the answer with a piece of paper and see if someone can solve it correctly.

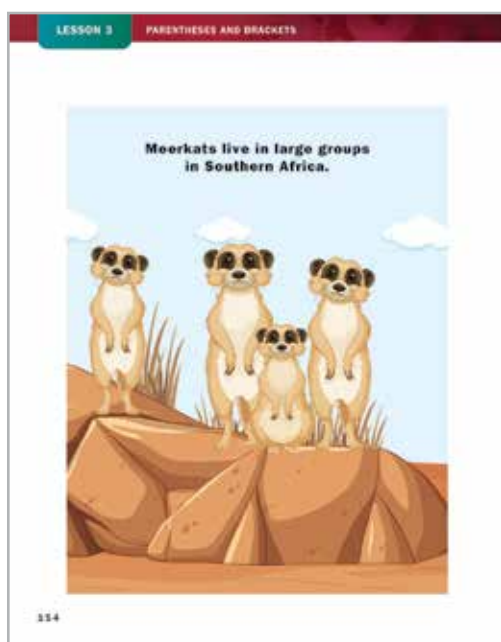
Answers will vary.

LESSON 3

The fraction bar, absolute value sign, and radical sign also function as grouping symbols in mathematics. But, they will be introduced at a higher level of mathematics. For now, students can focus on parentheses, braces, and brackets. Understanding the mathematical language and rules of these symbols is important for expanding your child's mathematical foundation.

For the opening activity, be sure to mix up the activity numbers. Your student should solve each problem before looking at the final picture on the back.

Activity Sheet Answers



Page 26 Answers

Page 26 Answers. The page features a red header with 'LESSON 3 PARENTHESES AND BRACKETS'. Below the header is a circular icon of a meerkat. The page contains the following content:

1. Evaluate each expression. Remember to follow the order of operations and complete steps within grouping symbols first. Show each step of your work.

The Order of Operations

1. Perform operations that are in grouping symbols such as parentheses.
2. Multiply and Divide (from left to right)
3. Add and Subtract (from left to right)

a. $(5 - 2) \times (4 + 5)$
 3×9
 27

b. $(25 \div 5) + (5 \times 4)$
 $5 + 24$
 29

c. $28 \div [10 - (5 \div 2)]$
 $28 \div [10 - 3]$
 $28 \div 7$
 4

d. $3 \times [(9 - 6) + (16 \div 2)]$
 $3 \times [3 + 8]$
 3×11
 33

e. $4 \times [(3 \times 3) - 5]$
 $4 \times [9 - 5]$
 4×4
 16

f. $2 \times [(12 - 8) \times 2] + 3$
 $2 \times [4 \times 2] + 3$
 $2 \times 8 + 3$
 $16 + 3$
 19

The page number '26' is in the bottom left corner.

LESSON 4

Exponents are introduced for the first time in this lesson, but only with 10 as the base. Note the common mistake of students is mixing up exponents with multiplication. To avoid this, they can write out the exponents as repeated multiplication until they become comfortable with the notation.

Page 27 Answers

LESSON 4: POWERS OF TEN

Roll, Write, and Expand

You Will Need:

- 3 dice

You Will Do:

- Roll the three dice and use the results to write a three-digit number below. Then write out the number in expanded form.
- Roll the three dice twice and write down a six-digit number in the space provided. Write out the number in expanded form.
- Roll the three dice three times and write down a nine-digit number. Write out the number in expanded form.

Sample Answers

Number	Expanded form
6 4 4	$600 + 40 + 4$
5 1 2 3 1 1	$500,000 + 10,000 + 2,000 + 300 + 10 + 1$
1 1 2 3 1 4 4 6 6	$100,000,000 + 10,000,000 + 2,000,000 + 300,000 + 10,000 + 4,000 + 400 + 60 + 6$

27

Page 30 Answers

LESSON 4: POWERS OF TEN

1. Use your knowledge of place value to answer the questions below.

- 800 is ten times as much as what number? **80**
- 90 is $1/10$ of what number? **900**
- 60,000 is ten times as much as what number? **6,000**
- 300 is $1/10$ of what number? **3,000**

2. Complete the chart.

Number	Ten times as much	$1/10$ as much
100	1,000	10
50	500	5
8,000	80,000	800
20,000	200,000	2,000
300,000	3,000,000	30,000

3. Match each number to the correct power of ten.

100	10^1
10	10^2
10,000	10^3
1,000,000	10^4
1,000	10^5
100,000	10^6

30

LESSON 5

All of this practice with powers of ten and moving numbers left and right also prepares students for multiplying decimals. We will build on this concept in the decimals unit using some of the same strategies. For now, the goal is to help your student become proficient and comfortable with the process.

Page 31 Answers

LESSON 5: POWERS OF TEN AND EXPANDED FORM

Powers of Ten Slider

You Will Need:

- Lesson 5: Activity Sheets
- Scissors

You Will Do:

- Carefully cut out the activity sheets from the back of the answer key. Cut out the black strips along the dotted lines. Then cut out the slider and cut along the dotted lines. The easiest way to do this is to fold the slider in half and cut the dots, and then unfold it.
- Place one of the strips into the slider so that it shows through in all of the place value windows. Write in the number 5,122. Move the decimal point in the number one space to the right by sliding the strip to the left. This also gives you the answer to $5,122 \times 10$. Write the answer below.
 $5,122 \times 10 =$ **51,220**
- Move the decimal point again by sliding the strip to the left one space to find the answer to $5,122 \times 100$. Write the answer below.
 $5,122 \times 100 =$ **512,200**
- Slide a new strip into the slider and write the number 98,000. This time we are going to move the decimal point to the left. Slide the strip to the right one space to find the answer to $98,000 \div 10$. Slide it to the right again to find the answer to $98,000 \div 100$. Write both answers below.
 $98,000 \div 10 =$ **9,800** $98,000 \div 100 =$ **980**
- Slide a third strip into the slider and write a number of your choosing. Slide it to the right and to the left to write and answer two of your own problems.
Answers will vary. _____ $\div 10 =$ _____ _____ $\div 100 =$ _____
- Keep the slider in a safe place; you will use it again in Lesson 8.

31

LESSON 5 POWERS OF TEN AND EXPANDED FORM

You've already learned one way to write numbers in expanded form. There are two other ways you can do this that help you see the place value relationship in different ways.

EXAMPLE 1: Write the number 76,839 in expanded form using multiplication and parentheses.
 $(7 \times 10,000) + (6 \times 1,000) + (8 \times 100) + (3 \times 10) + (9 \times 1)$

Writing the number out in expanded form like this lets us see each power of ten. We can also write numbers in expanded form using the powers of ten notation.

EXAMPLE 2: Write the number 76,839 in expanded form using the powers of ten.
 $7 \times 10^4 + 6 \times 10^3 + 8 \times 10^2 + 3 \times 10^1 + 9$

5. Use what you learned in the opening activity to find the answers to these problems. You can make a new strip and act it out if you need to.

a. $3,557 \times 10 = 35,570$

b. $3,557 \times 100 = 355,700$

c. $790,000 \div 10 = 79,000$

d. $790,000 \div 100 = 7,900$

POWERS OF TEN AND EXPANDED FORM LESSON 5

2. Write each number in expanded form using multiplication and parentheses.

a. 5,871 $(5 \times 1,000) + (6 \times 100) + (7 \times 10) + (1 \times 1)$

b. 10,196 $(1 \times 10,000) + (1 \times 100) + (5 \times 10) + (6 \times 1)$

c. 99,678 $(9 \times 10,000) + (9 \times 1,000) + (6 \times 100) + (7 \times 10) + (8 \times 1)$

d. 566,123 $(5 \times 100,000) + (6 \times 10,000) + (6 \times 1,000) + (1 \times 100) + (2 \times 10) + (3 \times 1)$

3. Write the each number in expanded form using the powers of ten.

a. 6,799 $6 \times 10^3 + 7 \times 10^2 + 9 \times 10^1 + 9$

b. 11,255 $1 \times 10^4 + 1 \times 10^3 + 2 \times 10^2 + 5 \times 10^1 + 5$

c. 345,115 $3 \times 10^5 + 4 \times 10^4 + 5 \times 10^3 + 1 \times 10^2 + 1 \times 10^1 + 5$

d. 90,221 $9 \times 10^4 + 2 \times 10^3 + 2 \times 10^1 + 1$

4. A researcher estimates that about 291,640 platypuses live in a region of Australia. Write this estimate in expanded form using multiplication and parentheses. Then write it again using powers of ten.

$(2 \times 100,000) + (9 \times 10,000) + (1 \times 1,000) + (6 \times 100) + (4 \times 10)$

$2 \times 10^5 + 9 \times 10^4 + 1 \times 10^3 + 6 \times 10^2 + 4 \times 10^1$

The platypus is an egg-laying, semi-aquatic mammal. They have many unique and surprising characteristics that don't match with what we typically assume about mammals.

LESSON 6

Scientific notation isn't typically introduced in 5th grade, but it is such a great application of what they have been learning that I wanted to include it. However, you will notice that I simplified it significantly. I haven't used any numbers that would involve decimals. For now, I just wanted them to practice with writing the powers of ten. This exposure will also make it easier for them to grasp the full concept when they come across it in a science book.

LESSON 6 SCIENTIFIC NOTATION

LESSON 6: SCIENTIFIC NOTATION

Powers of Ten Matching Activity

You Will Need:

- Lesson 6 Activity Sheet
- Scissors
- Glue stick

You Will Do:

- Carefully tear out the activity sheet from the back of the answer key.
- Cut apart the cards and scramble them.
- Match them to their correct spots. Glue your answers from the opening activity in the spaces below.

100	10^2
One hundred	10×10
1,000,000	10^6
One million	$10 \times 10 \times 10 \times 10 \times 10 \times 10$

Page 35 Answers

SCIENTIFIC NOTATION LESSON 6	
100,000	10^5
One hundred thousand	$10 \times 10 \times 10 \times 10 \times 10$
10,000	10^4
Ten thousand	$10 \times 10 \times 10 \times 10$
1,000	10^3
One thousand	$10 \times 10 \times 10$

35

Page 37 Answers

SCIENTIFIC NOTATION LESSON 6

1. Write each number in scientific notation.

a. 900 9×10^2

b. 8,000 8×10^3

c. 4,000 4×10^3

d. 70,000 7×10^4

e. 8,000,000 8×10^6

f. 300,000 3×10^5

2. Write the each number in standard form.

a. 3×10^4 30,000

b. 6×10^3 6,000

3. A researcher estimated that there were 400,000 African elephants. Write this number in scientific notation.

4×10^5

African elephant

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LESSON 7

Students are encouraged to solve the problems in this lesson in their own way. Let them try several strategies before you offer a possible method. There is more than one method that can be used, and you want your child to be competent in selecting the style that fits his or her learning style. Sample answers are provided below as a guide if your child needs your help.

Problem #1

One method that can work well with this problem is to make a list. Clue number 2 narrows down the options quite a bit, so begin by making a list of two-digit numbers that have a repeated digit.

11

22

33

44

55

66

77

88

99

Page 41 Answers

PROBLEM SOLVING PRACTICE LESSON 7

Solve each problem below using any strategy you like. Once you find the answer, explain what you did to your parent.

1. Elijah is thinking of a number. He gives 3 clues. Can you guess his number?

My number is a two-digit number.
Both digits are the same number.
The digits add up to 12.

66

2. Sam is playing with the six numbered cards shown below. He uses the card to make a subtraction problem with a difference of 854. If each card was only used once, where did he place each card in the problem?

1	3	5
7	9	0

$$\begin{array}{r} 957 \\ - 103 \\ \hline 854 \end{array}$$

41

Already we realize that we only have 9 options on our list. The third clue states that the digits must add up to 12. We can test each item on the list.

$$1 + 1 = 2$$

$$3 + 3 = 6$$

$$5 + 5 = 10$$

$$2 + 2 = 4$$

$$4 + 4 = 8$$

$$6 + 6 = 12$$

66

This is the only number on our list that will work.

Problem #2

A great method for this problem is guess-and-check. Writing the digits on pieces of paper or notecards that can be easily moved around helps with making the guesses easier to check. Suppose you guessed this first:

$$\begin{array}{r} 709 \\ - 531 \\ \hline 178 \end{array}$$

This guess is not correct. Also, you can see that the ones digits were not correct because we need a 4 in the ones column. On the next guess we will focus on getting the ones correct. Assuming there isn't any regrouping, $7 - 3$ is the only way to get a 4 in the ones column.

$$\begin{array}{r} 507 \\ - 193 \\ \hline 314 \end{array}$$

The ones digit is correct, but the answer is too small. The easiest way to increase the difference is to move the 9 digit to the hundreds place.

$$\begin{array}{r} 907 \\ - 153 \\ \hline 774 \end{array}$$

We are close. Let's try rearranging one more time.

$$957$$

Hooray! We found the answer.

$$\begin{array}{r} 957 \\ - 103 \\ \hline 854 \end{array}$$

COMPLETE SUPPLY LIST

- A four-operation calculator (add, subtract, multiply, and divide)
- Fraction tiles
- Pattern blocks
- Base ten blocks
- Linking Cubes
- A protractor
- Notecards
- Uno cards
- Masking tape
- A prize
- Scissors
- Tape
- 3 dice
- A glue stick
- Play money (\$1's, \$10's, and \$100's)
- Glue
- 15 one-inch square tiles
- Graham crackers
- Pretzel sticks
- Markers or colored pencils
- A clipboard
- 8 envelopes
- A timer
- Bingo chips or markers
- A timer
- Dominoes
- 30 counters
- Colored pencils
- 2 oranges (or another fruit that can be cut into thirds)
- 2 graham crackers
- 3 friends, siblings, dolls, stuffed animals or action figures
- Straws
- Paper clips
- 100 pennies
- 10 dimes
- A ruler
- 4 clear plastic bottles with caps
- A permanent marker
- A funnel
- 3 cups warm water
- Active dry yeast
- Sugar
- Table salt
- 6 balloons
- Popcorn
- 3 containers that are different sizes
- 1 cup measuring cup
- 50 cubes (such as the unit cubes in the base ten set)
- Game pieces
- 2 or more players
- 2 plastic bottles (16 ounces)
- 8 plastic bottle caps that are all the same size
- Skewers
- 2 rubber bands
- Knife and the help of an adult
- Times table
- Store flyers showing sales
- Coupons or online ads
- Food items in your refrigerator
- A collection of small objects (like a silverware drawer, a chess set, etc.)
- A bag of Skittles®
- A bag of M & M's® (or another small candy or snack)
- 10 people to survey
- Books or internet resources on animals
- Snack mix (any mixed bag of trail mix that has a variety of items in it)
- A cup
- A paper towel
- A tape measure
- 10 pencils (that are different lengths)
- Outdoor thermometer or weather website
- A bag of marshmallows
- A microwave
- A centimeter/inch ruler
- 2 posters
- Markers
- Chalk
- A plastic shower curtain or tablecloth
- Assorted toys
- Markers (dry erase or washable; depending on what kind of surface you are using)
- 5 magnets